R for Statistics and Graphics

Session 3

R for Inferential Statistics (Hypothesis Testing)
I. Categorical Data Analysis

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Outline

Useful R Features and Functions

Some Basic Statistical Concepts

Categorical Data Analysis



Generating a Simulated Vector

You can generate vectors of different kinds

```
seq(1:100)
                          # To have sequential numbers from 1 to 100 in a vector
seq(from=1, to=3, by=0.1) # To have a series of sequential numbers starting from 1 to 3
                            and increasing by 0.1
                          # To generate four random numbers within the default range
runif(4)
                            of 0 to 1
runif(10, min=1, max=100) # To generate 10 random numbers within the range 1 to 100
rnorm(n, mean = 0, sd = 1) # To generate "n" number of random numbers fitting to
                            normal distribution with default mean=0 and sd=1
rnorm(25, 30, 5)  # To generate a sample of size 25 from a normal
                            distribution with mean 30 and standard deviation 5
a <- rbinom(100, 10, 0.5) # 100 people tossing a fair coin (third argument=0.5) 10
                            times
                          # mean(a) should be close to 10*0.5 = 5
c(1,5,3,8)
                          # to create a vector of these numbers
```



Generating a Simulated Dataset

```
# Generate a dataset/dataframe for a case-control study:
       cc <-
       data.frame(case.id = 1:100,
       age = rnorm(100, mean = 60, sd = 12),
       caco = gl(2, 50, labels = c("Case", "Control")))
       summary (cc)
   case.id age
                                    caco
Min. : 1.00 Min. : 29.40 Case :50
1st Qu.: 25.75 1st Qu.: 54.31 Control :50
Median: 50.50 Median: 61.24
Mean : 50.50 Mean : 61.29
3rd Qu.: 75.25 3rd Qu.: 66.22
Max. :100.00 Max. :102.47
```



Generating a Simulated Dataset

Generate a dataset with multiple random variables:

```
set.seed(955)
   vvar < -1:20 + rnorm(20, sd=3)
   wvar < -1:20 + rnorm(20, sd=5)
   xvar < -20:1 + rnorm(20, sd=3)
   yvar < (1:20)/2 + rnorm(20, sd=10)
   zvar <- rnorm(20, sd=6)</pre>
   data <- data.frame(vvar, wvar, xvar, yvar, zvar)</pre>
   head (data)
#>
         vvar
                    wvar
                             xvar
                                        yvar
                                                  zvar
#> 1 -4.252354 5.1219288 16.02193 -15.156368 -4.086904
#> 2 1.702318 -1.3234340 15.83817 -24.063902 3.468423
#> 3 4.323054 -2.1570874 19.85517 2.306770 -3.044931
#> 4 1.780628 0.7880138 17.65079 2.564663 1.449081
#> 5 11.537348 -1.3075994 10.93386 9.600835 2.761963
#> 6 6.672130 2.0135190 15.24350 -3.465695 5.749642
```



rxc Contingency Table

How to Create a Contingency Table

```
x <- matrix(c(22, 46, 66, 58), nrow = 2) #To create a 2x2 table
     OR
                      # Assign a name to the contingency table to be created
x <- data.frame()
                      # Opens the data editor to enter the cell values (rxc)
fix(x)
                      # Prints the newly created contingency table
X
         var1 var2
     1 34
               42
         22
               11
To run for example, Fisher's test, use the assigned name of the 2x2 table (x):
fisher.test(x)
To edit the contingency table (or any spreadsheet), use:
                       # Opens the data editor to edit the cell values
edit(x)
```



Factors for Grouping

Factors are grouping variables (like gender, age group or nationality) and can be used to create subsets (strata) of data for subset-specific analysis http://uc-r.github.io/factors

Let's use another built-in dataframe for an exercise



Factors for Grouping

```
data(infert)
    str(infert)
'data.frame': 248 obs. of 8 variables:
$ education : Factor w/ 3 levels "0-5yrs", "6-11yrs", ..: 1 1 1 1 2 2 2 2 2 2 ...
$ age
              : num 26 42 39 34 35 36 23 32 21 28 ...
$ parity
              : num 6 1 6 4 3 4 1 2 1 2 ...
             : num 1 1 2 2 1 2 0 0 0 0 ...
$ induced
$ case
              : num 1 1 1 1 1 1 1 1 1 1 ...
$ spontaneous : num 2 0 0 0 1 1 0 0 1 0 ...
$ stratum
                : int 1 2 3 4 5 6 7 8 9 10 ...
$ pooled.stratum: num 3 1 4 2 32 36 6 22 5 19 ...
    infert$case <- as.factor(infert$case)</pre>
    str(infert)
'data.frame': 248 obs. of 8 variables:
$ education : Factor w/ 3 levels "0-5yrs", "6-11yrs", ..: 1 1 1 1 2 2 2 2 2 2 ...
$ age
        : num 26 42 39 34 35 36 23 32 21 28 ...
$ parity : num 6 1 6 4 3 4 1 2 1 2 ...
$ induced : num 1 1 2 2 1 2 0 0 0 0 ...
$ case
          : Factor w/ 2 levels "0","1": 2 2 2 2 2 2 2 2 2 ...
$ spontaneous
                : num 2 0 0 0 1 1 0 0 1 0 ...
$ stratum
                : int 1 2 3 4 5 6 7 8 9 10 ...
$ pooled.stratum: num 3 1 4 2 32 36 6 22 5 19 ...
The "case" variable is now a factor. You can also check this with:
    class(infert$case)
[1] "factor"
```



Factors for Grouping

```
x <- table(infert$case, infert$spontaneous)</pre>
      X
              2
0 113 40 12
1 28 31 24
      summary(table(infert$case, infert$spontaneous))
Number of cases in table: 248
Number of factors: 2
Test for independence of all factors:
         Chisq = 32.86, df = 2, p-value = 7.314e-08
The variable "case" is numeric:
      summary(infert)
  education
                            parity
                                        induced
                                                        case
                                                                  spontaneous
                                                                                  stratum
                                                                                            pooled.stratum
 0-5yrs: 12 Min. :21.00 Min. :1.000 Min. :0.0000 Min. :1.000 Min.
                                                                      :0.0000
                                                                               Min. : 1.00 Min. : 1.00
 6-11yrs:120 1st Qu.:28.00
                         1st Qu.:1.000 1st Qu.:0.0000 1st Qu.:1.000
                                                                1st Qu.:0.0000
                                                                               1st Qu.:21.00
                                                                                            1st Qu.:19.00
12+ vrs:116 Median:31.00 Median:2.000 Median:0.0000 Median:1.000
                                                                Median :0.0000
                                                                               Median:42.00
                                                                                            Median :36.00
            Mean :31.50 Mean :2.093 Mean :0.5726 Mean :1.335
                                                               Mean :0.5766
                                                                               Mean :41.87 Mean :33.58
            3rd Qu.:35.25 3rd Qu.:3.000 3rd Qu.:1.0000 3rd Qu.:2.000
                                                                3rd Qu.:1.0000
                                                                               3rd Qu.:62.25
                                                                                            3rd Qu.:48.25
            Max. :44.00 Max. :6.000 Max. :2.0000 Max. :2.000
                                                                                            Max. :63.00
                                                               Max. :2.0000
                                                                               Max. :83.00
The variable "case" is factor "infert$case <- as.factor(infert$case)":
      summary(infert)
  education
                            parity
                                                                                      pooled.stratum
                                         induced
                                                    case
                                                           spontaneous
                                                                           stratum
 0-5vrs : 12 Min. :21.00
                         Min. :1.000
                                      Min. :0.0000
                                                    1:165
                                                          Min. :0.0000
                                                                        Min. : 1.00
                                                                                     Min. : 1.00
 6-11yrs:120
           1st Qu.:28.00
                         1st Qu.:1.000 1st Qu.:0.0000
                                                   2: 83
                                                         1st Qu.:0.0000 1st Qu.:21.00
                                                                                     1st Qu.:19.00
            Median:31.00
12+ yrs:116
                         Median :2.000 Median :0.0000
                                                           Median :0.0000
                                                                        Median:42.00
                                                                                     Median :36.00
            Mean :31.50
                         Mean :2.093
                                      Mean :0.5726
                                                           Mean :0.5766
                                                                        Mean :41.87
                                                                                     Mean :33.58
                                                                                     3rd Qu.:48.25
            3rd Qu.:35.25
                         3rd Qu.:3.000 3rd Qu.:1.0000
                                                           3rd Qu.:1.0000
                                                                        3rd Qu.:62.25
            Max. :44.00
                         Max. :6.000 Max. :2.0000
                                                           Max. :2.0000
                                                                        Max. :83.00
                                                                                     Max. :63.00
```



apply(), sapply(), lapply(), and tapply()

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apply(), sapply(), tapply() in R with Examples

This tutorial aims at introducing the apply() function collection. The apply() function is the most basic of all collection. We will also learn sapply(), lapply() and tapply(). The apply collection can be viewed as a substitute to the loop

The apply() collection is bundled with **r essential** package if you install R with Anaconda. The apply() function can be feed with many functions to perform redundant application on a collection of object (data frame, list, vector, etc.). The purpose of apply() is primarily to avoid explicit uses of loop constructs. They can be used for an input list, matrix or array and apply a function. Any function can be passed into apply().



R RDocumentation

Search for packages, functions, etc.

R Enterprise Training

R package

Leaderboa

Apply Functions Over Array Margins

Returns a vector or array or list of values obtained by applying a function to margins of an array or matrix.

Keywords array, iteration

Usage

```
apply(X, MARGIN, FUN, ...)
```

Arguments

X an array, including a matrix.

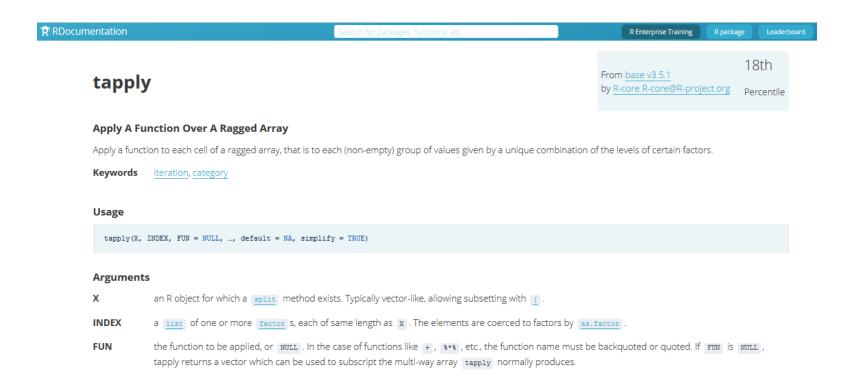
MARGIN a vector giving the subscripts which the function will be applied over. E.g., for a matrix 1 indicates rows, 2 indicates columns, c(1, 2) indicates rows

and columns. Where | x| has named dimnames, it can be a character vector selecting dimension names.

FUN the function to be applied: see 'Details'. In the case of functions like +, ***, etc., the function name must be backquoted or quoted.



tapply()



The tapply () function is useful when we need to break up a vector into groups defined by some classifying factor, compute a function on the subsets, and return the results in a convenient form.

```
data(iris)
tapply(iris$Petal.Length, iris$Species, mean)
    setosa versicolor virginica
    1.462    4.260    5.552
```



aggregate()

Aggregate Multiple Columns At Once

The formula method of the aggregate () function allows running the same function on multiple columns at once (like the apply () function). The formula is the first argument of the function: "." represents all variables other than the grouping factor (like Species in iris). The grouping factor is defined on the right hand side of (~). Second argument is the dataframe name, and the third is the function to be applied.



with()

The with() function applys an expression to a dataset. It is similar to DATA= in SAS.

```
# with(data, expression)
# example applying a t-test to a data frame mydata
with(mydata, t.test(y ~ group))
```

```
data(infert)
with(infert, t.test(infert$parity ~ infert$case))
# parity is a count variable and case is the case-
control indicator (grouping factor)
```



with



by

Apply A Function To A Data Frame Split By Factors

A data frame is split by row into data frames subsetted by the values of one or more factors, and function FUN is applied to each subset in turn.

```
data(iris)
by (iris$Sepal.Length, iris$Species, summary) # summary statistics of
                            Sepal.Length is requested for each Species
iris$Species: setosa
  Min. 1st Qu. Median Mean 3rd Qu. Max.
 4.300 4.800 5.000
                        5.006
                               5.200
                                      5.800
iris$Species: versicolor
                       Mean 3rd Qu.
  Min. 1st Qu. Median
                                       Max.
 4.900
         5.600
                5.900
                        5.936
                               6.300
                                       7.000
iris$Species: virginica
  Min. 1st Qu. Median Mean 3rd Qu.
                                      Max.
 4.900 6.225 6.500
                        6.588
                               6.900
                                      7.900
```



R Function of the Day

Variables: Equivalent Terms

Input
Independent
Explanatory
Exposure
Predictor
Regressor



Output
Dependent
Response
Outcome
Predicted
Regressand

Co-variate (Potential) Confounder



Effect Size

The strength/magnitude/degree of a correlation/association is assessed by the effect size.

The *P* value is a measure of statistical significance (or the strength of statistical significance). The effect size is the measure (and <u>not</u> the *P* value) to use to compare two results.

RR / OR / HR / ARR / NNT
Correlation coefficient
Cohen's d value *
Regression coefficient

* https://www.rdocumentation.org/packages/DescTools/versions/0.99.19/topics/CohenD



Statistical Tests

No adjustment	With adjustment			
Chi-squared or Exact test	(Logistic) regression			
t-test	Multivariable regression			
Log-rank test (survival test)	Cox regression			
Correlation	Multivariable regression			
Linear regression	Multivariable regression			
ANOVA - Linear regression				



Statistical Tests for Categorical Data (rxc Table) Analysis

Test	Context
Chi-squared or exact test	Observed counts in groups
McNemar's test	Observed counts in groups, but matched data
Goodness-of-fit test	Observed counts and expected proportions
Mantel-Haenszel test	Multiple rxc tables are analyzed simultaneously (like a meta-analysis)
Trend test (Cochran-Mantel-Haenszel test)	Observed counts in at least three groups
Z-test	An observed proportion and an hypothesized proportion; or two observed proportions



Count Data Analysis

Define your $r \times c$ table as a matrix; assign a name to it (e.g., mymatrix), and enter your matrix name within the brackets:

```
chisq.test(mymatrix)
fisher.test(mymatrix)
mcnemar.test(mymatrix) # For matched observations
```

Define your array as multiple matrices; assign a name to it (e.g., myarray), and enter your array name within the brackets:

```
cmh . test (myarray) # The array is multiple contingency tables
```

Define the first column of your table (exposed) in a vector (x) and the totals for each category in a different vector (n) for the trend test:

```
prop. trend. test (x, n) # Like smokers (x) out of total subjects (n)
```

Define a vector of your observed counts (x), and a vector of expected proportions (p) for the goodness-of-fit test:

```
chisq.test(x, p=p) # Note that x is counts, and p is proportions
```



Count Data Analysis

R for Categorical Data Analysis

Steele H. Valenzuela

Using R for Biomedical Statistics

Biomedical statistics

This booklet tells you how to use the R software to carry out some simple analyses that are common in biomedical statistics. In particular, the focus is on cohort and case-control studies that aim to test whether particular factors are associated with disease, randomised trials, and meta-analysis.

This booklet assumes that the reader has some basic knowledge of biomedical statistics, and the principal focus of the booklet is not to explain biomedical statistics analyses, but rather to explain how to carry out these analyses using R.

A Little Book of R For Biomedical Statistics

Release 0.2



Count Data Analysis

2.4 Testing for an Association Between Disease and Exposure, in a Cohort or Case-Control Study

In a case-control or cohort study, it is interesting to do a statistical test for association between having the disease and being exposed to some treatment or environment (for example, smoking or taking a certain drug).

In R, you can test for an association using the Chi-squared test, or Fisher's exact test. For example, using our data from the example above:

```
> print (mymatrix)
          Disease Control
Exposure1
               30
                       24
              76
                      241
Exposure2
Unexposed
                      509
> chisq.test(mymatrix)
     Pearson's Chi-squared test
 data: mymatrix
 X-squared = 60.5762, df = 2, p-value = 7.015e-14
> fisher.test(mymatrix)
    Fisher's Exact Test for Count Data
 data: mymatrix
 p-value = 5.263e-12
 alternative hypothesis: two.sided
```

Here the P-value for the Chi-squared test is about 7e-14, and the P-value for Fisher's exact test is about 5e-12. Both are very tiny (<0.05), indicating a significant association between exposure and disease (using a cutoff of P<0.05 for statistical significance).



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Count Data Analysis

2.5 Calculating the (Mantel-Haenszel) Odds Ratio when there is a Stratifying Variable

You may have data from a cohort study or case-control study that is stratified, for example, the data may be separated (stratified) by the sex of the people studied. For example, we may have two different tables giving information on the relationship between exposure (eg. to a certain drug or smoking cigarettes) and having a particular disease. One of the tables may given information for women, and the other give information for men.

••••••••••••••••••••••••••••••

Requires the R package "lawstat"

This tells you that the odds ratio for the first stratum (women) is 16.480, the odds ratio for the second stratum (men) is 28.667, and the aggregate odds ratio that we would get if we pooled the data for men and women is 25.550. The Mantel-Haenszel odds ratio is estimated to be 23.001.

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Dose Response (Trend) Test

In a dose-response analysis, it is usual to have information on the incidence of a disease in people who were exposed to different doses of some factor (for example, number of cigarettes smoked per day, dose of a certain drug taken, etc.). For example, your data may look like this:

	Disease	Control
Dose=2	35	82
Dose=9.5	250	293
Dose=19.5	196	190
Dose=37	136	71
Dose=50	32	13

We can enter our data into R as follows (note that you need to type "nrow=5" to tell R that there are 5 rows of data):

```
> mymatrix <- matrix(c(35,82,250,293,196,190,136,71,32,13),nrow=5,byrow=TRUE)</pre>
> colnames(mymatrix) <- c("Disease", "Control")</pre>
> rownames(mymatrix) <- c("2", "9.5", "19.5", "37", "50")</pre>
> print (mymatrix)
       Disease Control
 2
            35
                    82
 9.5
           250
                   293
 19.5
           196
                   190
 37
           136
                    71
 50
            32
                    13
```

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More suited for epidemiological analysis

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Count Data Analysis

Dose Response (Trend) Test

prop.trend.test

From stats v3.5.3 by R-core R-core@R-project.org Percentile

99.99th

Test For Trend In Proportions

Performs chi-squared test for trend in proportions, i.e., a test asymptotically optimal for local alternatives where the log odds vary in proportion with score. By default, score is chosen as the group numbers.

```
> prop.trend.test(x = c(47, 31, 9, 5), n = c(49, 40, 18, 10))
        Chi-squared Test for Trend in Proportions
data: c(47, 31, 9, 5) out of c(49, 40, 18, 10) ,
using scores: 1 2 3 4
X-squared = 21.031, df = 1, p-value = 4.519e-06
```



R for Categorical Data Analysis

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Count Data Analysis

Dose Response (Trend) Test

. ptrendi 47 2 1 \ 31 9 2 \ 9 9 3 \ 5 5 4

	г	nr	_prop	x
1.	47	2	0.959	1.00
2.	31	9	0.775	2.00
3.	9	9	0.500	3.00
4.	5	5	0.500	4.00

Stata output

```
Trend analysis for proportions
```

```
Regression of p = \mathbf{r}/(\mathbf{r}+\mathbf{nr}) on x:

slope = -.18261, std. error = .03982, Z = 4.586

Overall chi2(3) = 22.407 pr>chi2 = 0.0001

chi2(1) for trend = 21.031 pr>chi2 = 0.0000

chi2(2) for departure = 1.376, pr>chi2 = 0.5026
```

```
R output
```

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Dose Response (Trend) Test

EXERCISE:

Define x and n for the following command to work correctly:

prop.trend.test(x, n)



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Count Data Analysis

Dose Response (Trend) Test

EXERCISE:

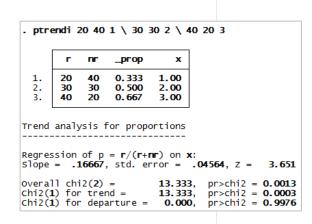
Define x and n for the following command to work correctly:

```
prop.trend.test(x, n)
```

```
x = c(20, 30, 40)
n = c(60, 60, 60)
prop.trend.test(x,n)

Chi-squared Test for Trend in Proportions

data: x out of n ,
    using scores: 1 2 3
X-squared = 13.333, df = 1, p-value = 0.0002607
```





Count Data Analysis

Dose Response (Trend) Test

Generate a matrix:

```
matrix1 <- matrix(c(35, 82, 250, 293, 196, 190, 136, 71, 32,
13), nrow=5, byrow=TRUE)
colnames(matrix1) <- c("cases", "controls")
rownames(matrix1) <- c("0", "1", "2", "3", "4+")
matrix1  # to inspect the matrix with row and column names included</pre>
```

cases controls 0 35 82 1 250 293 2 196 190 3 136 71 4+ 32 13

Run DescTools:MHChisqTest()

```
MHChisqTest(matrix1)
```

```
Mantel-Haenszel Chi-Square
data: matrix1
X-squared = 47.158, df = 1, p-value = 6.55e-12
```

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Count Data Analysis

Goodness-of-fit Test

#Conducting a one-way chi-square (replace stars with appropriate observed frequencies e.g 26,31,26,27 obtained from step 1 and expected ratio as proportions e.g.,1/4,1/4,1/4) chisq.test(c(**,**,**,**),p=c((*/*),(*/*),(*/*)))

3. Identifying the key elements of the output

Following the instructions above will produce the following output in the **R Console** window: the **key elements** are annotated in blue.

```
> #Importing data from tab delimited file (replace stars with an appropriate object name e.g.,peas)
> peas<-read.table(file.choose(),header=TRUE)
> attach(peas)
> names(peas)
[1] "form"
            "colour" "category"
> #Calculating observed frequencies (replace stars with approriate text eg., category, category)
> tapply(category,category,length)
  Round.Green Round.Yellow Wrinkled.Green Wrinkled.Yellow
26 31 26 27 NOTE: Use these frequencies generated by
                                                step 1 in the code in step 2
> #Conducting a one-way chi-square (replace stars with appropriate observed frequencies and expected
ratio as proportions e.g 26,31,26,27 and 1/4,1/4,1/4)
> chisq.test(c(26,31,26,27),p=c((1/4),(1/4),(1/4),(1/4)))
     Chi-squared test for given probabilities
data: c(26, 31, 26, 27)
X-squared = 0.6182, df = 3, p-value = 0.8923
Statistic
                 Degrees of Freedom
                                                P Value
```



Count Data Analysis

Goodness-of-fit Test

For paired or matched count data, ordinary Chi-squared test is not appropriate, and McNemar's test should be used.

Define the matrix for your 2x2 table, and run the test as shown.

```
> mcnemar.test(mymatrix)
    McNemar's Chi-squared test with continuity correction

data: mymatrix
McNemar's chi-squared = 26.4143, df = 1, p-value = 2.755e-07
```



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Count Data Analysis

Z-test

Not much different from Chi-squared test; it is used to compare a proportion with an hypothesized proportion (one-sample test), or to test the equality of two proportions (two-sample test).

prop.test

Exact And Approximate Tests For Proportions

```
prop.test(x, n, p = NULL, alternative = c("two.sided", "less",
    "greater"), conf.level = 0.95, data = NULL, success = NULL, ...)
```

```
prop.test(76, 100, 0.50) # One-sample Z-test

1-sample proportions test with continuity correction
data: 76 out of 100, null probability 0.5
X-squared = 26.01, df = 1, p-value = 3.397e-07
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
    0.6623089 0.8373345
sample estimates:
    p
0.76
```

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Count Data Analysis

Z-test

```
prop.test(c(76, 50), c(100, 100)) # If continuity correction
                is not needed, correct = FALSE argument can be added
    2-sample test for equality of proportions with continuity
    correction
data: c(76, 50) out of c(100, 100)
X-squared = 13.406, df = 1, p-value = 0.0002508
alternative hypothesis: two.sided
95 percent confidence interval:
 0.1211184 0.3988816
sample estimates:
prop 1 prop 2
 0.76 0.50
1-sample proportions test with continuity correction
data: 76 out of 100, null probability 0.5
X-squared = 26.01, df = 1, p-value = 3.397e-07
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
   0.6623089 0.8373345
sample estimates:
0.76
```



Count Data Analysis

Now, run

Script: s3.R



2x2 Table Analysis

Information that can be obtained from a 2x2 table

Association statistics

(Chi-squared and Fisher's exact test)

Effect size

(Odds ratio, relative risk, absolute risk reduction, number needed to treat)

Measures of diagnostic accuracy

(Sensitivity, specificity, positive/negative predictive tests, ROC/AUC)

Association measures

(Phi coefficient, Cramer's V, Yule's Q and others)

Now, run

Script: contingency.R



Next

R for Inferential Statistics

II. t-test, ANOVA, regression

